

# False Discoveries in Mutual Fund Performance: Measuring Luck in Estimated Alphas

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Laurent Barras\*, Olivier Scaillet\* & Russ Wermers\*\*

\*FAME, University of Geneva

\*\*University of Maryland



# Outline

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- Motivations
- Contribution & Results
- False Discovery Rate
- Performance Measurement & Data
- Empirical Results
- Conclusion

# Motivations

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- On average, the mutual fund industry underperforms
  - Lehman and Modest (1987), Elton et al. (1993), Pastor and Stambaugh (2002)...
- But do some funds generate differential performance, namely positive or negative alphas?
- Standard approach developed in the literature:
  1. Each fund estimated alpha is tested by computing its  $p$ -value
  2. A fund is significant if its  $p$ -value is smaller than a chosen significance level  $\gamma$
  3. The number of significant funds provides an estimator of the number of funds with positive or negative performance
  - Proposed by Jensen (1968), Ferson and Schadt (1996), Ferson and Qian (2004)

# Motivations

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- Every test on fund alpha is subject to luck
  - A lucky fund is a fund with a significant estimated alpha while its true alpha is equal to zero
- The standard approach implies multiple testing across all funds
  - If  $\gamma$  is set to 0.05, the probability of finding at least one lucky fund is much higher than 5%!
  - Grinblatt and Titman (1995): «While some funds achieved **positive abnormal** returns, it is difficult to ascertain the implications of this for the efficient market hypothesis because of **multiple comparison** being made. That is, even if **no** superior management ability existed, we would expect some funds to achieve **superior** risk-adjusted returns **by chance**. »
- Therefore, the standard approach cannot account for luck!

# Motivations

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Test of differential performance among 1'500 funds

## *Question 1: Impact of Luck on Performance?*

- At  $\gamma=0.05$ , 50 funds have positive significant alphas
- Do all of them truly yield positive alphas?

## *Question 2: Variation of the significance level $\gamma$ ?*

- At  $\gamma=0.10$ , 80 funds have positive significant alphas
- Do the 30 new significant funds produce positive alphas?

## *Question 3: Comparisons across investment categories?*

- Two categories: Growth and Growth & Income
- The number of funds with positive significant alphas is identical
- Is the real performance across the two categories the same?

# Contributions & Results

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- Measuring the impact of luck on mutual fund performance
- False Discovery Rate (FDR)
  - The proportion of lucky funds among any group of significant funds
  - Easy to compute from the individual fund  $p$ -values provided by the standard approach
- **New methodology** to measure the FDR among the best and worst funds
  - The best funds are funds with positive significant alphas (right tail)
  - The worst funds are funds with negative significant alphas (left tail)
- Answering the previous questions by computing the FDR:
  - Across different significance levels  $\gamma$  (0.05, 0.10...)
  - Across different investment categories (All, G, AG, GI)

## Contributions & Results

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### *Answer to Question 1: Impact of Luck on Performance?*

- Luck has a stronger impact on the performance of the best funds

### *Answer to Question 2: Variation of the significance level $\gamma$ ?*

- As  $\gamma$  rises, the FDR among the best funds increases quickly, while the FDR among the worst funds increases slowly

### *Answer to Question 3: Comparisons across investment categories?*

- The AG funds obtain the best performance, while the GI funds generate the worst one
  - The standard approach concludes that 7.7% of the GI funds have positive performance. Accounting for luck, none of them can achieve a positive performance. Clearly a False Discovery!!

# False Discovery Rate (FDR)

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## A. The Standard Approach: A Three-Step Procedure

1. Test of differential performance for each fund  $i$  ( $i=1,\dots,M$ ):

$$H_0 : \alpha_i = 0,$$

$$H_A : \alpha_i > 0 \text{ or } \alpha_i < 0$$

- $\alpha_i$  is computed with a given asset pricing model
- The individual  $p$ -values can be computed with asymptotic theory or bootstrap techniques (Koswoski et al. (2005))

2. Fund  $i$  is called significant if its  $p$ -value is smaller than  $\gamma$

# False Discovery Rate (FDR)

## A. The Standard Approach: A Three-Step Procedure

3. The number of funds with non-zero alphas is estimated by the number  $R(\gamma)$  of significant funds
- This approach cannot distinguish between luck and differential performance:

➤  $R(\gamma) = F(\gamma) + T(\gamma)$

Lucky funds (or False Discoveries) →  $F(\gamma)$

$T(\gamma)$  → Funds with differential performance (i.e.  $\alpha_i > 0$  or  $\alpha_i < 0$ ),

## False Discovery Rate (FDR)

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### B. The False Discovery Rate: Only One More Step

4. From the fund  $p$ -values, we simply compute the FDR
  - The FDR is defined as the proportion of lucky funds among the significant funds:

$$FDR(\gamma) = E \left( \frac{F(\gamma)}{R(\gamma)} \middle| R(\gamma) > 0 \right)$$

- It is a simple extension of the standard approach
  - We can then measure the impact of luck through  $\hat{F}(\gamma) = \widehat{FDR}(\gamma) \cdot \hat{R}(\gamma)$
  - We can estimate the number of funds with non-zero alphas:  $\hat{T}(\gamma) = \hat{R}(\gamma) - \hat{F}(\gamma)$

# False Discovery Rate (FDR)

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## C. FDR among the Best and Worst Funds

- We suggest to use a **new** methodology designed to measure the proportion of lucky funds among the best and worst funds :
  - $R^+$  is the number of funds with positive estimated alphas, namely the best funds
  - $R^-$  is the number of funds with negative estimated alphas, namely the worst funds
  - Because we use a equal-tailed, two-sided test, we expect that under  $H_0$ :

$$\begin{array}{l}
 \begin{array}{l}
 \nearrow 1/2 \\
 F \\
 \searrow 1/2
 \end{array}
 \begin{array}{l}
 F^+ \\
 \\
 F^-
 \end{array}
 \begin{array}{l}
 \longrightarrow \\
 \\
 \longrightarrow
 \end{array}
 \begin{array}{l}
 FDR^+(\gamma) = E \left( \frac{F^+(\gamma)}{R^+(\gamma)} \middle| R^+(\gamma) > 0 \right) \\
 \\
 FDR^-(\gamma) = E \left( \frac{F^-(\gamma)}{R^-(\gamma)} \middle| R^-(\gamma) > 0 \right)
 \end{array}
 \end{array}$$

# False Discovery Rate (FDR)

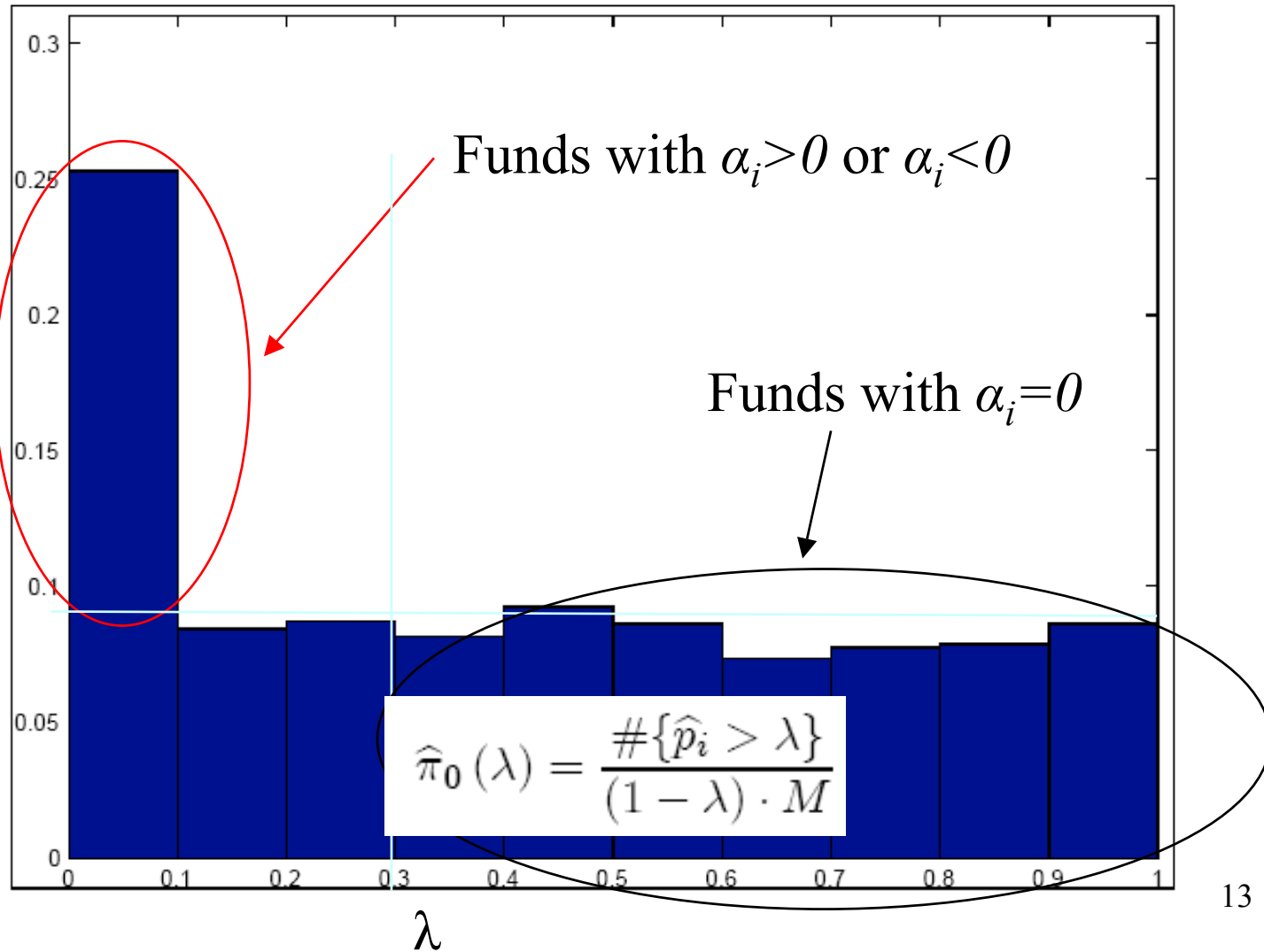
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## D. Estimation Procedure

- The estimator: 
$$\widehat{FDR}_\lambda(\gamma) = \frac{M \cdot \widehat{\pi}_0(\lambda) \cdot \gamma}{\#\{\widehat{p}_i < \gamma\}} = \frac{\widehat{F}(\gamma)}{\widehat{R}(\gamma)}$$
- $M$  denotes the number of funds in the population
- $\pi_0$  is the proportion of funds with  $\alpha_i=0$
- $\gamma$  is the significance level
- $\widehat{p}_i$  is the fund  $i$  estimation  $p$ -value
- The estimation procedure is trivial once we have  $\pi_0$

# False Discovery Rate (FDR)

Histograms of 1'500 fund  $p$ -values



## A. Performance Measurement

- Baseline asset pricing model (Carhart model):

$$r_{i,t} = \alpha_i + b_i \cdot r_{m,t} + s_i \cdot r_{smb,t} + h_i \cdot r_{hml,t} + m_i \cdot r_{mom,t} + \varepsilon_{i,t}$$

- Fund  $p$ -values are computed by bootstrap technique
  - Kosowski et al. (2005)
- Use of the  $t$ -stat instead of the alpha
  - Better statistical properties for the bootstrap (higher order improvements)
  - Reduce the impact of extreme alphas

## B. Data

- Monthly returns of U.S. open-end equity funds from CRSP between 1975 and 2002
  - Wermers (2000), Kosowski et al. (2005)
- Investment objectives by Thomson Financial
  - Wermers (2000)
- 1'472 All // 1'025 G // 234 AG // 310 GI funds

# Empirical Results

## A. The Standard Approach (All funds)

$\gamma$	0.05	0.10	0.15	0.20
$R^+$	52	83	112	140
$\hat{R}^-$	104	165	234	282

1) Do these significant funds truly yield non-zero alphas?

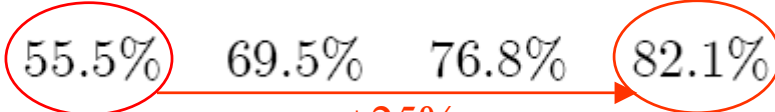

2) Are these new significant funds all performing?

- We need to assess the impact of luck, i.e. the proportion of lucky funds among the different groups of significant funds!<sup>16</sup>

## B. Using the FDR (All funds)

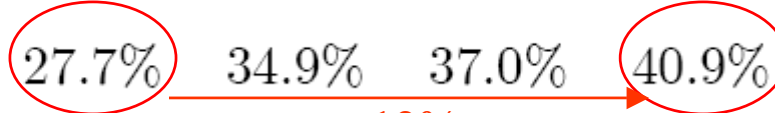
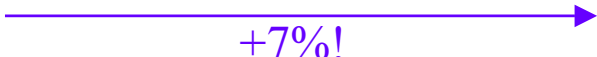
### Best funds

$\gamma$	0.05	0.10	0.15	0.20
$\widehat{FDR}^+$	55.5%	69.5%	76.8%	82.1%
$\widehat{R}^+$	52 ?	83	112	139
$\widehat{F}^+$	29	58	87	116
$\widehat{T}^+$	23	25	25	25

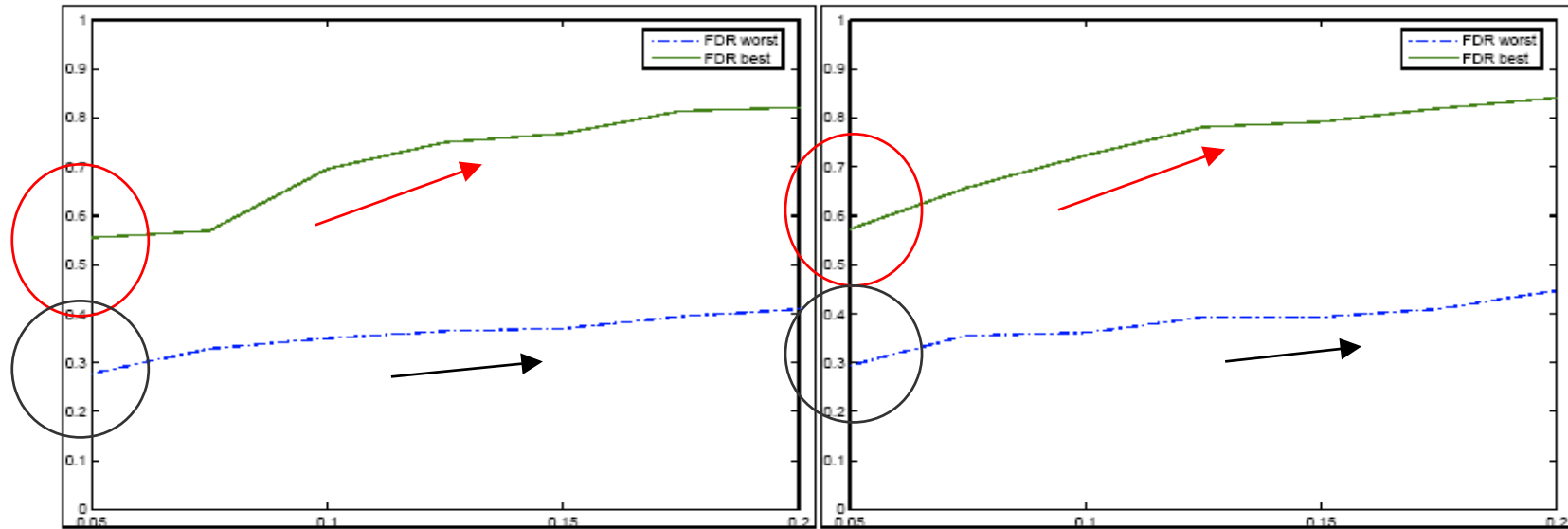

  


### Worst funds

$\gamma$	0.05	0.10	0.15	0.20
$\widehat{FDR}^-$	27.7%	34.9%	37.0%	40.9%
$\widehat{R}^-$	104 ?	165	234	283
$\widehat{F}^-$	29	58	87	116
$\widehat{T}^-$	75	107	147	167

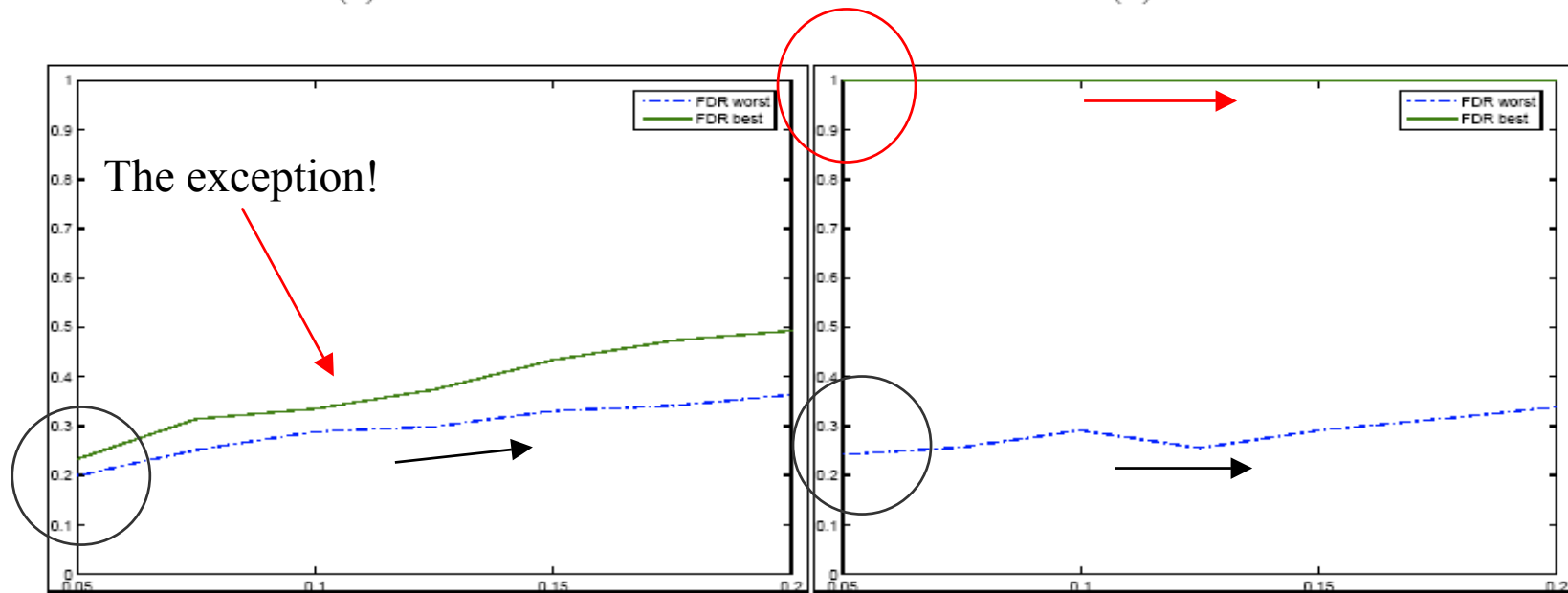

  


## False Discovery Rates among the Best and the Worst Funds



(a) All funds

(b) G funds



(c) AG funds

(d) GI funds

# Empirical Results

## Implications for Mutual Fund Performance Analysis

	Positive performance $\hat{\pi}_A^+$	Negative performance $\hat{\pi}_A^-$
<i>All</i> funds	1.9%	19.6%
<i>G</i> funds	1.5%	18.0%
<i>AG</i> funds	8.1%	20.3%
<i>GI</i> funds	0.0%	24.3%

- The negative average mutual fund performance is caused by the poor performance of 20% of the funds!
- AG funds perform well, while GI funds represent a striking evidence of false discovery!!

# Conclusion

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- Can some funds achieve differential performance?
- To answer this question, we need to measure the impact of luck on performance due to multiple testing
- This is done by using the False Discovery Rate (FDR)
  - Proportion of lucky funds among a given group of significant funds
  - Straightforward extension of the standard approach developed in the literature: very easy to implement while giving much insight into the individual performance of mutual funds

# Conclusion

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- Luck has a stronger impact on the performance of the best funds
  - The FDR among the best funds is high and rises quickly
  - The FDR among the worst funds is low and rises slowly
  
- However, a tiny fraction of funds yield positive performance
  - 1.5% of the All and G funds (more pronounced for *AG* funds)
  - These funds are located at the extreme right tail of the cross-sectional distribution of alpha

## Additional Results

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- Is this tiny evidence sufficient to form portfolios of the best funds which generate positive alphas?
- Yes, because the best funds are located at the extreme right tail of the cross-sectional alpha distribution
  - They can be separated from the non-performing funds by setting a low  $\gamma$
  - Implications for the selection procedure in the fund of fund industry
- Moreover, the FDR has wide application: it can be used every time a test is run a large number of times
  - Test of predictability
  - Performance of technical trading rules (Sullivan et al. (1999))